

L9(4.6) - Factoring Strategies

Consider the factoring methods we have explored so far:

1. Common Factors $3x^2 + 6x + 9$
2. Factoring by Grouping $ac + ad + bc + bd$
3. Simple Trinomials $x^2 + bx + c$
4. Complex Trinomials $ax^2 + bx + c, a \text{ not } 1$
5. Perfect Square Trinomials $a^2 + 2ab + b^2$
6. Difference of Squares $a^2 - b^2$

It is often sufficient to use only one method, but there are times when they must be combined. This occurs most often when **common factors** are involved.

Break it down further:

1. Common Factors and Grouping
2. Perfect or Difference of squares
3. Trinomials

Look for these!!!!

Always check for common factors before you start **and** after you think you are done.

When you are asked to "fully factor" or "factor completely", all common factors must also be accounted for.

Ex.1 Remove Common Factors First and Last

$$\begin{aligned} &= 4(x^2 - 5x + 6) \quad \begin{array}{l} 4x^2 - 20x + 24 \\ \hline = 4x^2 - 8x - 12x + 24 \\ = 4x(x-2) - 12(x-2) \\ = (4x-12)(x-2) \\ = 4(x-3)(x-2) \end{array} \end{aligned}$$

Ex.2 Determine the best strategies required to factor:

(a) $x^2 + 8x + 15$

Simpler

$$= (x+3)(x+5)$$

(d) $4x^2 + 8x + 4$

4) $64 = 2^6$ Perfect Square

$$= 4(x^2 + 2x + 1)$$

$$= 4(x+1)(y+1)$$

$$= 4(x+1)^2 / (x+1)^2$$

(b) $6x^2 + 19x + 8$

Complex

Complex

$$= 6x^2 + 3x + 16x + 8$$

$$= (3x+8)(2x+1)$$

(c) $40x^2 - 250$

GCF of 10

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(e) $9x^2 + 48x + 64$

$+1)$ Perfect Square

$$= (3x+8)(3x+8)$$

$$= (3.49)^2$$

$$= (7x + 8)$$

(f) $-3x^2 + 60x + 180$

6CF
perfect square

$$= \frac{1}{2} (x^2 - (x+3)^2)$$

$$= -5(x-6)^2$$

$$= 10(4x^2 - 25)$$

Assigned Work: p. 236 # 1, (6-8)ace, 9, 10, 12, 14ac, 17*

$$= 10(z_x + 5)(z_x - 5)$$

$$= (20x + 50)(2x - 5)$$

$$= 40x^2 - \underbrace{100x + 100x}_{0} - 250$$